

# Labor Market Frictions, Human Capital Accumulation, and Consumption Inequality

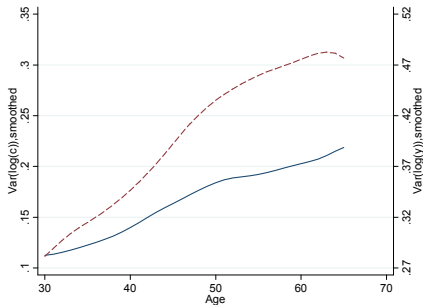
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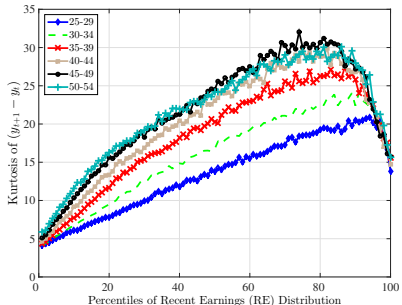
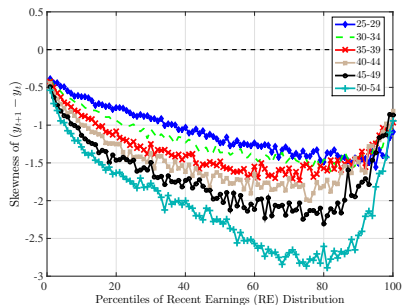
HCEO Conference on Human Capital and Inequality  
University of Chicago  
December 16-17, 2015

# Introduction

- What is the relative contribution of shocks to human capital accumulation and the stochastic job ladder in determining the uncertainty workers face in the labor market?



source: Meghir & Pistaferri (2011)



source: Guvenen, Karahan, Ozkan and Song (2015)

## Related Literature

- **Statistical models of income processes**

Lillard and Willis (1978); Lillard and Weiss (1979); MaCurdy (1982); Abowd and Card (1989); Topel and Ward (1992); Gottschalk and Moffit (1995); Baker and Solon (2003); Meghir and Pistaferri (2004); Guvenen (2007); Altonji, Smith and Vidangos (2013); Guvenen, Karahan, Ozkan and Song (2015); Arellano, Blundell and Bonhomme (2015).

- **Choices, information and risk**

Deaton and Paxson (1994); Blundell and Preston (1998); Krueger and Perri (2004); Storesletten, Telmer, and Yaron (2004); Cunha, Heckman and Navarro (2005); Blundell, Pistaferri and Preston (2008); Kaplan and Violante (2010); Lise (2013); Guvenen and Smith (2013) ...

- **Job-search, learning and human capital accumulation**

Rubinstein and Weiss (2006); Yamaguchi (2010); Burdett, Carrillo-Tudela and Coles (2011); Bowlus and Liu (2013); Bagger, Fontaine, Postel-Vinay and Robin (2014); Lise and Postel-Vinay (2015)

# Model Ingredients

## Equilibrium random search model of the labour market

- Time is continuous, workers are risk averse, discount the future at rate  $\rho$ , and exit the market at rate  $\xi$
- Workers search for jobs when unemployed and for better jobs when employed
- Firms recruit new workers and counter outside offers to retain their existing workers

## Worker and firm heterogeneity

- Differences in ability/productivity
- Human capital accumulation depends on worker and firm type

## Incomplete markets (Aiyagari-Beweley-Huggett)

- No complete set of state-contingent claims
- Single riskless asset to transfer resources over time

## Technology

A match between a worker of type  $\mathbf{h}_t$  and a firm of type  $y$  produces

$$f(\mathbf{h}_t, y) = h_0 h_{1t} y$$

The worker supplies **human capital**  $\mathbf{h}_t = \{h_0, h_{1t}\}$

- fixed worker type  $h_0$
- time-variant human capital  $h_{1t}$

The firm is characterized by the **fixed productivity type**  $y$

Home production takes the form

$$b(\mathbf{h}_t) = h_0 h_{1t} b$$

# Human Capital Accumulation

The time varying component  $h_{1t}$  follows a diffusion process:

$$\frac{dh_{1t}}{h_{1t}} = \mu(h_0, y)dt + \sigma d\mathcal{B}_t,$$
$$\mu(h_0, y) = \mu_0 + \mu_1 \log h_0 + \mu_2 \log y$$

## Human capital accumulation

- The drift rate depends on the current match.
- It is assumed to be non-decreasing in the firm-type.

## Idiosyncratic productivity- and health shocks

- Deviations from the deterministic path are captured by the Brownian motion  $\mathcal{B}_t$  with diffusion parameter  $\sigma$

## Meetings and Transitions

- Search is random and sequential.
- Both employed and unemployed workers are contacted by a firm at type dependent **contact rate**

$$\lambda(h_0) = \exp(\lambda_0 + \lambda_1 \log h_0)$$

and receive offers from the **sampling distribution**

$$\Gamma(y) \quad y \in [\underline{y}, \bar{y}]$$

the decision to accept or reject the offer is endogenous

- A worker becomes unemployed at type dependent **separation rate**

$$\delta(h_0) = \exp(\delta_0 + \delta_1 \log h_0)$$

and leaves the labor market at rate

$\xi$



## Wages

The wage is assumed to be a **piece-rate**  $0 < \theta \leq 1$  of match output:

$$w_t = h_0 h_{1t} y \theta_t$$

$$\log w_t = \log h_0 + \log y + \log h_{1t} + \log \theta_t$$

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Firms compete based on current output:

Suppose a worker currently matched with firm  $y$  is contacted by a firm of type  $y'$ :

- if  $y' > y$  the worker moves to firm  $y'$  and the piece rate there starts at

$$\theta' = \frac{y}{y'}$$

- if  $y \geq y'$  the worker stays at  $y$  and the piece rate is updated to

$$\theta = \max \left\{ \theta, \frac{y'}{y} \right\}$$

## Worker Values

Worker with assets  $a$ , human capital  $(h_0, h_1)$ , matched to firm  $y$ , at piece-rate  $\theta$ :

$$\begin{aligned} & [\rho + \lambda(h_0) + \delta(h_0) + \xi]W(a, h_0, h_1, y, \theta) \\ &= \max_{a - \underline{a} \geq c \geq 0} u(c) + \frac{\partial}{\partial a} W(a, h_0, h_1, y, \theta)[ra + \theta h_0 h_1 y - c] \\ &+ \mu(h_0, y) h_1 \frac{\partial}{\partial h_1} W(a, h_0, h_1, y, \theta) + \frac{\sigma^2}{2} h_1^2 \frac{\partial^2}{\partial h_1^2} W(a, h_0, h_1, y, \theta) \\ &+ \lambda(h_0) \int \max \left\{ W(a, h_0, h_1, y', y/y'), \right. \\ &\quad \left. W(a, h_0, h_1, y, \max\{\theta, y'/y\}) \right\} d\Gamma(y') \\ &+ \delta(h_0)W(a, h_0, h_1, b, 1) + \xi R(a, h_0, h_1) \end{aligned}$$

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# Data

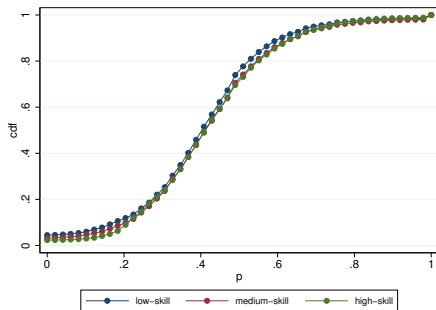
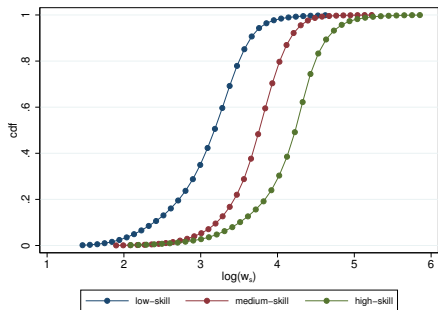
- Linked Employer-Employee data from Germany spanning the years 1975-2010
  - ▶ 2% random sample consisting of 212,380 male workers who started their career during the sample
  - ▶ worker id, firm id, wages, worker flows,...
- Income and Expenditure Survey (EVS)
  - ▶ Repeated cross-section carried out every 5 years starting from 1978

▶ Details

# Identification

- Worker types  $h_0$  are identified from their first wage
- Firms are ranked and binned into types based on the share of workers they hire from other firms; The sampling distribution is identified from job types accepted out of unemployment
- $\delta(h_0)$  and  $\lambda(h_0)$  are identified by separation rates and unemployment rates, conditional on  $h_0$
- Human capital accumulation (type dependent mean and variance) is identified using three job spells using the difference in starting wages between spell 2 and 3. (If spell 1 and 2 are at the same firm type it is especially helpful)

# Estimated Distribution of Worker Types and Firm Types

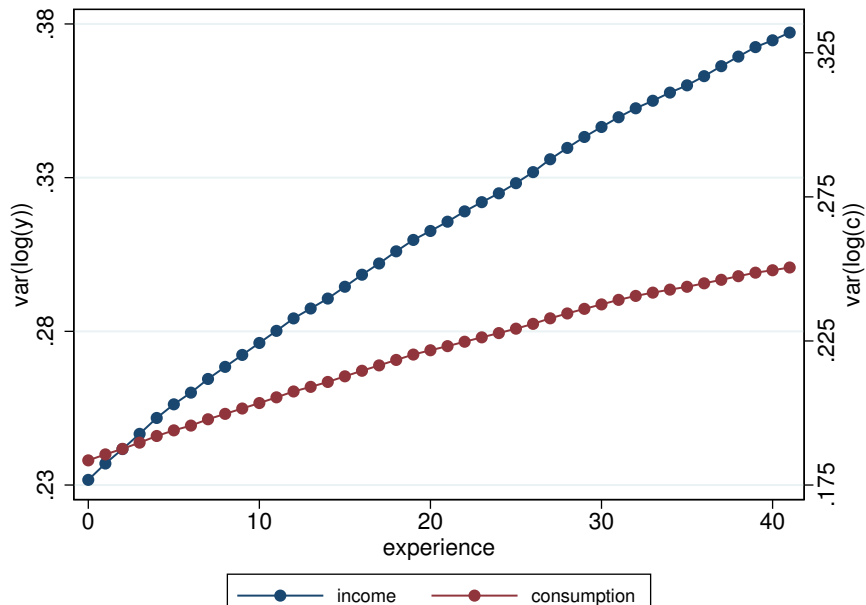


## Parameter Estimates (preliminary)

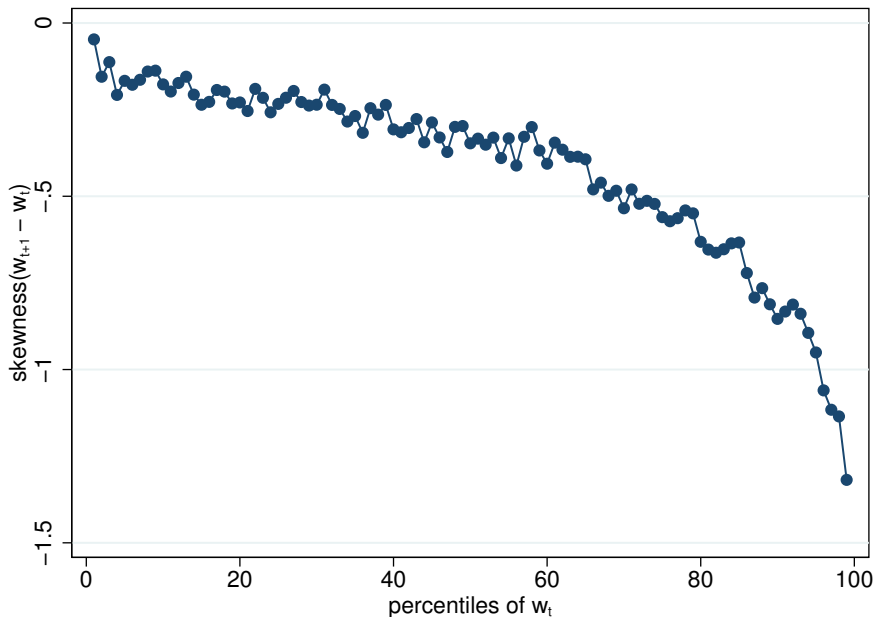
	low-skilled	high-skilled
Contact rates: $\lambda(h_0) = \exp(\lambda_0 + \lambda_1 \log h_0)$		
$\lambda_0$	-2.632	-2.733
$\lambda_1$	-0.0910	-0.1102
Destruction rates: $\delta(h_0) = \exp(\delta_0 + \delta_1 \log h_0)$		
$\delta_0$	-3.585	-4.912
$\delta_1$	0.1316	-0.345
Human capital, drift: $\mu(h_0, y) = \mu_0 + \mu_1 \log h_0 + \mu_2 \log y$		
$\mu_0$	0.000	0.000
$\mu_1$	-0.003	-0.0034
$\mu_2$	0.001	0.0025
Human capital, variance of shocks: $\sigma^2$		
$\sigma^2$	0.0174	0.02007



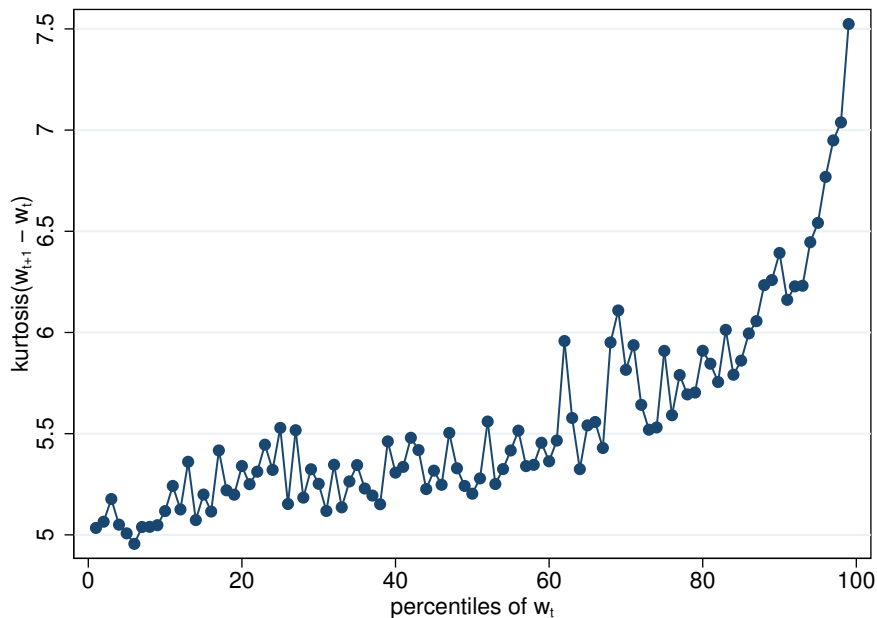
## Linear increase in earnings and consumption variance



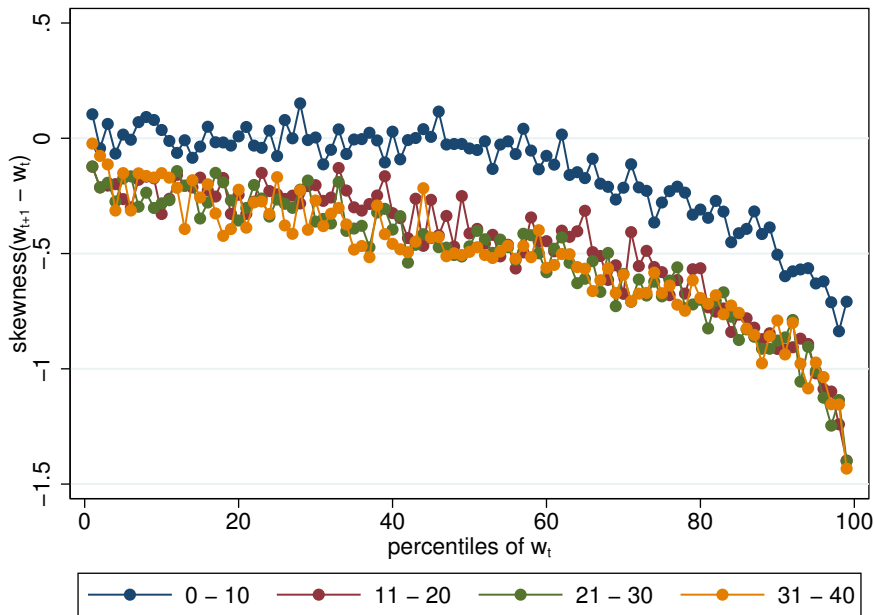
# Negative skewness of $\Delta w_{t+1}$ , decreasing in $w_t$



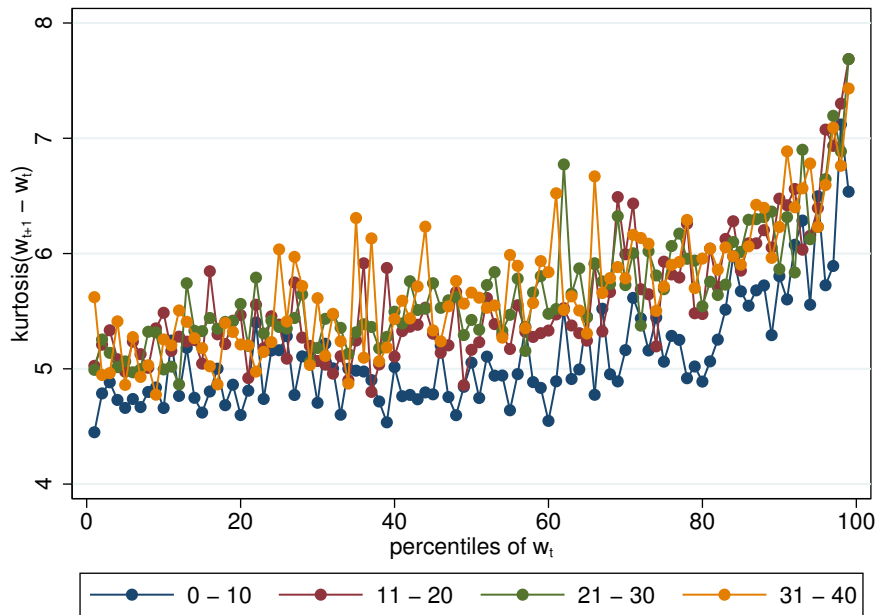
## Excess Kurtosis of $\Delta w_{t+1}$ , increasing in $w_t$



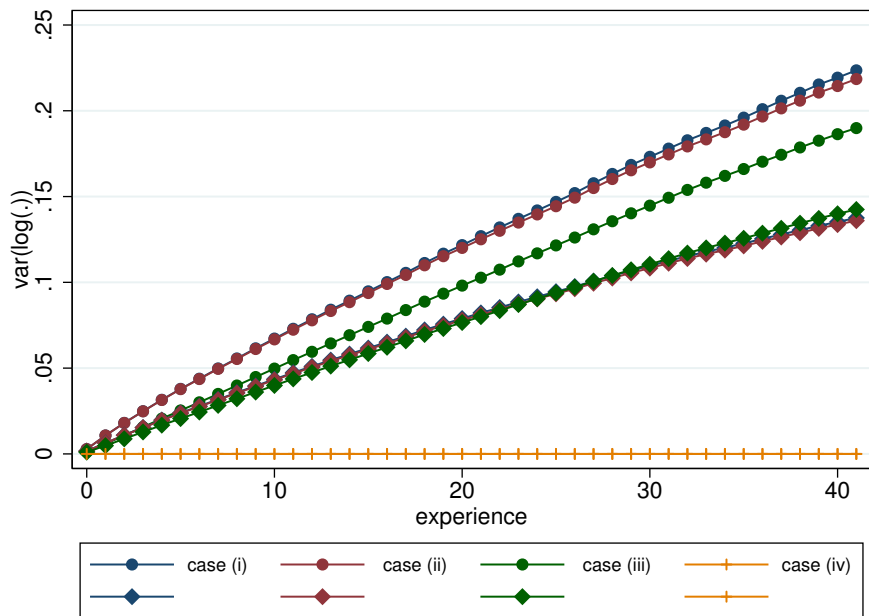
# Negative skewness of $\Delta w_{t+1}$ , decreasing with experience(?)



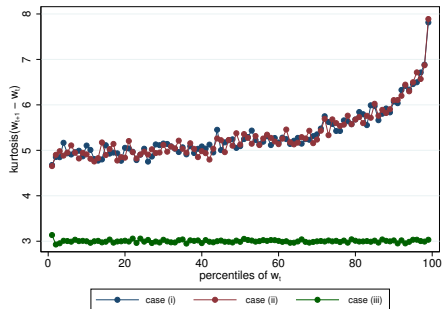
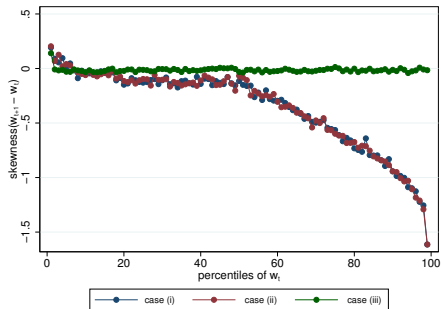
# Excess Kurtosis of $\Delta w_{t+1}$ , increasing with experience(?)



# Rising variance is almost all due to shocks to human capital



# Skewness and Kurtosis almost all due to job ladder



# Conclusion

- Persistent shocks account for the rising variance of log earnings and consumption
- The job ladder accounts qualitatively for the patterns of the skewness and kurtosis of conditional year-over-year wage changes
- Our preliminary results do not produce the quantitative patterns of the skewness and kurtosis using loss of search capital alone
- We conjecture loss of human capital at job loss will beef up the quantitative effects





# Linked Employer-Employee Data: SIAB 7510 & BHP

## Employment Spells

- reported with exact start- and end-dates
- spells can end for a number of reasons: changes in the wage paid, changing employer, switching to part-time,...

## Wages and Hours

- Wages are provided by firms and are very accurate due to the threat of legal sanctions for misreporting.
- Hours are not reported, but information on full-time, long and short part-time work.
- The reported wages are average daily wages for each spell.
- **Drawback:** Top-coding at the social security contribution limit.

## Worker Flows

- worker-flows at the establishment level from the Establishment History Panel (BHP)

# Sample Restrictions

Sample of **labour market entrants** between 1975-2010:

- males based in West-Germany
- age restrictions upon entry
- divided into three mutually exclusive skill groups

Based on the employment spell data, we generate a panel data set at monthly frequency.

- spells that last for less than one month are dropped.
- unemployment is proxied by non-employment

# Income and Expenditure Survey (EVS)

- Federal Statistical Office (Destatis)
- Repeated cross-section carried out every 5 years starting from 1978.
- Detailed household and consumption data.
- Information on earnings and income.
- Large representative sample of around 60,000 households.